Extragalactic Radio Sources and the WMAP Cold spot

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ABSTRACT

We detect a dip of 20-45\% in the surface brightness and number counts of NVSS sources smoothed to a few degrees at the location of the WMAP cold spot. The dip has structure on scales of $\sim 1^\circ$ to $10^\circ$. Together with independent all-sky wavelet analyses, our results suggest that the dip in extragalactic brightness and number counts and the WMAP cold spot are physically related, i.e., that the coincidence is neither a statistical anomaly nor a WMAP foreground correction problem. If the cold spot does originate from structures at modest redshifts, as we suggest, then there is no remaining need for non-Gaussian processes at the last scattering surface of the CMB to explain the cold spot. The late integrated Sachs-Wolfe effect, already seen statistically for NVSS source counts, can now be seen to operate on a single region. To create the magnitude and angular size of the WMAP cold spot requires a $\sim 140$ Mpc radius completely empty void at $z\leq 1$ along this line of sight. This is far outside the current expectations of the concordance cosmology, and adds to the anomalies seen in the CMB.

Subject headings: large-scale structure of the universe – cosmic microwave background – radio continuum: galaxies

1. Introduction

The detection of an extreme “cold spot” (Vielva et al. 2004) in the foreground-corrected WMAP images was an exciting but unexpected finding. At $4^\circ$ resolution, Cruz et al. (2005) determine an amplitude of -73 $\mu$K, which reduces to -20 $\mu$K at $\sim 10^\circ$ scales (Cruz et al.

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The non-gaussianity of this extreme region has been scrutinized, (Cayon, Jun & Treaster 2005; Cruz et al. 2005, 2006, 2007) concluding that it cannot be explained by either foreground correction problems or the normal Gaussian fluctuations of the CMB. Thus, the cold spot seems to require a distinct origin – either primordial or local. Across the whole sky, local mass tracers such as the optical Sloan Digital Sky Survey (SDSS, York et al. 2000) and the radio NRAO VLA Sky Survey (NVSS, Condon et al. 1998) are seen to correlate with the WMAP images of the CMB (Pietrobon, Balbi & Marinucci 2006; Cabre et al. 2006), probably through the late integrated Sachs-Wolfe effect (ISW, Crittenden & Turok 1996).

McEwen et al. (2007) extended the study of radio source/CMB correlations by performing a steerable wavelet analysis of NVSS source counts and WMAP images. They isolated 18 regions that, as a group, contributed a significant fraction of the total NVSS-ISW signal. Three of those 18 regions were additionally robust to the choice of wavelet form. The centroid of one of those three robust correlated regions, (#16), is inside the 10° cold spot derived from WMAP data alone (Cruz et al. 2007), although McEwen et al. (2007) did not point out this association.

The investigations reported here were conducted independently and originally without knowledge of the McEwen et al. (2007) analysis. However, our work is a posteriori in nature, because we were specifically looking for the properties in the direction of the cold spot. These results thus support and quantify the NVSS properties in the specific direction of the cold spot, but should be considered along with the McEwen et al. (2007) analysis for the purposes of an unbiased proof of a WMAP association.

2. Analysis and Characterization of the NVSS “dip”

We examined both the number counts of NVSS sources in the direction of the WMAP cold spot and their smoothed brightness distribution. The NVSS 21 cm survey covers the sky above a declination of -40° at a resolution of 45”. It has an rms noise of 0.45 mJy/beam and is accompanied by a catalog of sources stronger than 2.5 mJy/beam. Because of the short interferometric observations that went into its construction, the survey is insensitive to diffuse sources greater than ≈ 15’ in extent. Convolution of the NVSS images to larger beam sizes, as done here, shows the integrated surface brightness of small extragalactic sources; this is very different than what would be observed by a single dish of equivalent resolution. In the latter case, the diffuse structure of the Milky Way Galaxy dominates (e.g, Haslam et al. 1981), although it is largely invisible to the interferometer.
To explore the extragalactic radio source population in the direction of the WMAP cold spot, we first show in Figure 1 the 50°×50° region around the cold spot convolved to a resolution of 3.4°. Here, the region of the cold spot is seen to be the faintest region on the image (minimum at l_{II}, b_{II} = 207.8°, -56.3°). At minimum, its brightness is 14 mK below the mean, with an extent of ≈5°. The WMAP cold spot thus picks out a special region in the NVSS – at least within this 2500° region.

We examined the smoothed brightness distribution across the whole NVSS survey using another averaging technique that reduces the confusion from the brightest sources. We first pre-convolved the images to 800", which fills all the gaps between neighboring sources, and then calculated the median brightness in sliding boxes 3.4° on a side. The resulting image is shown in Figure 2 which is in galactic coordinates centered at l_{II}=180°. The dark regions near the galactic plane are regions of the NVSS survey that were perturbed by the presence of very strong sources. Note that the galactic plane itself, which dominates single dish maps, is only detectable here between -20° < l_{II} < 90°, where there is a local increase in the number of small sources detectable by the interferometer.

To evaluate the NVSS brightness properties of the cold spot, we compared it with the distribution of median brightnesses in two strips from this all sky map. The first strip was in the north, taking everything above a nominal galactic latitude of 30° (More precisely, we used the horizontal line in the Aitoff projection tangent to the 30° line at l_{II}=180°.) The second strip was in the south, taking everything below a nominal galactic latitude of -30°, but only from 10° < l_{II} < 180°, to avoid regions near the survey limit of δ=-40°. The minimum brightness in the cold spot region (≈ 20 mK) is equal to the lowest values seen in the 16,800 square degree area of the two strips, and is ≈ 30% below the mean (Figure 3).

Formally, the probability of finding this weakest NVSS spot within the ≈10° (diameter) region of the WMAP cold spot is 0.6%. This a posteriori analysis thus is in agreement with the statistical conclusions of McEwen et al. (2007) that the NVSS properties in this region are linked to those of WMAP. We also note that the magnitude of the NVSS dip is at the extreme, but not an outlier of the overall brightness distribution. We thus expect that less extreme NVSS dips would also individually correlate with WMAP cold regions, although it may be more difficult to separate those from the primordial fluctuations.

The NVSS brightness dip can be seen at a number of resolutions, and there is probably more than one scale size present. At resolutions of 1°, 3.4°, and 10°, we find that the dip is ≈ 60%, 30% and 10% of the respective mean brightness. At 10° resolution, the NVSS deficit overlaps with another faint region about 10° to the west, while the average dip in brightness then decreases from -14 mK (at 3.4°) to -4 mK.
The dip in NVSS brightness in the WMAP cold spot region is not due to some peculiarity of the NVSS survey itself. In Figure 4, we compare the 1° convolved NVSS image with the similar resolution, single dish 408 MHz image of Haslam et al. (1981). This 408 MHz all sky map is dominated in most places by galactic emission, and was used by Bennett et al. (2003) as a template for estimating the synchrotron contribution in CMB observations. On scales of 1°, the fluctuations in brightness are a combination of galactic (diffuse) and extragalactic (smeared small source) contributions. In the region of the cold spot, we can see the extragalactic contribution at 408 MHz by comparison with the smoothed NVSS 1.4 GHz image. Note that although there is flux everywhere in the NVSS image, this is the “confusion” from the smoothed contribution of multiple small extragalactic sources in each beam, whereas the 408 MHz map has strong diffuse galactic emission as well. Strong brightness dips are seen in both images in the region of the WMAP cold spot - with the brightness dropping by as much as 62% in the smoothed NVSS; in the 408 MHz map, this is diluted by galactic emission.

To look more quantitatively at the source density in the cold spot region, we measured the density of NVSS sources (independent of their fluxes) as a function of distance from the cold spot. Figure 5 shows the counts in equal area annuli around the WMAP cold spot down to two different flux limits. With a limit of 5 mJy, there is a 45±8% decrease in counts in the 1° radius circle around the WMAP cold spot centroid. At the survey flux limit of 2.5 mJy, the decrease is 23±3%. This reduction in number counts is what is measured by McEwen et al. (2007) in their statistical all-sky analysis.

3. Foreground Corrections

Several studies have claimed that the properties of the cold spot are most likely an effect of incorrect foreground subtraction (Chiang & Naselsky 2004; Coles 2005; Liu & Zhang 2005; Tojeiro et al. 2006). This possibility has been investigated in detail for both the first year (Vielva et al. 2004; Cruz et al. 2005, 2006) and third (Cruz et al. 2007) year WMAP data. The arguments against foreground subtraction errors can be summarized in three main points – 1) The region of the spot shows no spectral dependence in the WMAP data. This is consistent with the CMB and inconsistent with the known spectral behavior of galactic emission (as well as the SZ effect). The flat (CMB-like) spectrum is found both in temperature and kurtosis, as well as in real and wavelet space. 2) Foreground emission is found to be low in the region of the spot, making it unlikely that an over-subtraction could produce an apparent non-Gaussianity. 3) Similar results are found when using totally independent methods to model and subtract out the foreground emission (Cruz et al. 2006),
namely the combined and foreground cleaned Q-V-W map (Bennett et al. 2003) and the weighted internal linear combination analysis (Tegmark et al. 2003).

Now that we know that there is a reduction in the extragalactic radio source contribution in the direction of the cold spot, we can re-examine this issue. We ask whether a 20-30% decrement in the local brightness of the extragalactic synchrotron emission could translate into a foreground subtraction problem that could generate the WMAP cold spot. We are not re-examining the foreground question \textit{ab initio}, simply examining the plausibility that the deficit of NVSS sources could complicate the foreground calculations in this location. The characteristic brightness in the 3.4° convolved NVSS image around the cold spot is \( \sim 51 \, \text{mK} \) at 1.4 GHz; the brightness of the cold spot is \( \sim 37 \, \text{mK} \). This difference of 14 mK in brightness (4 mK at 10° resolution) represents the extragalactic population contribution only, as the NVSS is not sensitive to the large scale galactic synchrotron emission. By contrast, the single dish 1.4 GHz brightness within a few degrees of the cold spot is \( \sim 3.4 \, \text{K} \), as measured using the Bonn Stockert 25 m telescope (Reich and Reich 1986). Therefore the total synchrotron contribution at 1.4 GHz is \( \sim 0.7 \, \text{K} \) above the CMB, 50 times larger than the localized extragalactic deficit.

One way to create the cold spot would be if the universal spectral index used for the normal galactic (plus small extragalactic) subtraction was incorrect for the \textit{extra} brightness temperature contribution of the NVSS dip, \( \delta T \) (-14 mK at L band, 1.4 GHz). We make an order of magnitude estimate of this potential error. Following the first year data analysis (Bennett et al. 2003), and the similar exercise performed by Cruz et al. (2006), we consider fitting a synchrotron template map at some reference frequency \( \nu_{\text{ref}} \), and extrapolating the model, \( F(\nu)_{\text{model}} \), with a spectral index of \( \beta = -3 \) to the Q, V, and W bands. This spectral index is consistent with those of Cruz et al. (2006) and the average spectral index observed in the WMAP images (Bennett et al. 2003; Hinshaw et al. 2006). Under the null hypothesis that the spectral index of \( \delta T \) is the same as that of the mean brightness \( T_0 \), we then calculate in the region of the deficit,

\[
F(\nu)_{\text{model}} = [T_0(\nu_{\text{ref}}) + \delta T(\nu_{\text{ref}})] (\nu/\nu_{\text{ref}})^{-3}.
\]  

However, if the actual spectrum of \( \delta T \) is \( -\alpha \) (from L band through W band) instead of -3, then the true foreground subtraction, \( F(\nu)_{\text{true}} \), should have been

\[
F(\nu)_{\text{true}} = T_0(\nu_{\text{ref}}) (\nu/\nu_{\text{ref}})^{-3} + \delta T(\nu_{\text{ref}}) (\nu/\nu_{\text{ref}})^{-\alpha}.
\]  

The foreground subtraction would then be in error as a function of frequency as follows,
expressed in terms of the L band temperatures:

\[
\delta F(\nu) \equiv F(\nu)_{\text{true}} - F(\nu)_{\text{model}} = \delta T(\nu_L/\nu)^\alpha \left[ 1 - (\nu_{\text{ref}}/\nu)^{3-\alpha} \right].
\] (3)

Three different reference frequencies have been used for synchrotron extrapolation— the Haslam et al. (1981) 408 MHz map (Bennett et al. 2003), the Jonas, Baart & Nicolson (1998) 2326 MHz Rhodes/HartRAO survey (Cruz et al. 2006), and the internal K and Ka band WMAP images (Hinshaw et al. 2006). Since the foreground subtraction errors would be worst extrapolating from the lowest frequency template, we start at 408 MHz and look at the problems caused by a spectral index for \(\delta T\) that is different than the assumed -3.

We obtain a rough measure of the spectral index of the dip by comparing the 1° resolution maps (Figure 4) at 408 MHz and 1400 MHz. At \(l_{II},b_{II} = 207^\circ,-55^\circ\), we find \(\delta T = 2.6\pm0.75\) K (30\(\pm12\) mK) at 408 (1400) MHz, yielding a spectral index of -3.6\(\pm0.5\). Using Equation (3), this would actually lead to a WMAP “hot spot” if a spectral index of -3.0 had been assumed for the extrapolation. Within the errors, the worst foreground extrapolation mistakes would then be hot spots that range from +0.5 to +4.6 \(\mu\)K at Q band, 1° resolution, (\(\approx +0.25\) to +2.3 \(\mu\)K at 4° resolution). Our derived spectral index for the dip is steeper than expected for extragalactic sources, so we also do the calculation assuming the flattest reasonable extragalactic spectrum of -2.5. This would lead to a spurious cold spot of -2.9 \(\mu\)K at 4° resolution. In either case, this is far below the -73 \(\mu\)K observed at this resolution in WMAP, and we thus conclude that the deficit of NVSS sources does not lead to a significant foreground subtraction error of either sign.

4. Discussion

The WMAP cold spot could have three origins: a) at the last scattering surface \((z \sim 1000)\), b) cosmologically local \((z < 1)\), or c) galactic. Because the spot corresponds to a significant deficit of flux (and source number counts) in the NVSS, we have argued here that the spot is cosmologically local and hence, a localized manifestation of the late ISW effect.

Cruz et al. (2005, 2007) derived a temperature deviation for the cold spot of \(-20\mu K\) and a diameter of 10° using the WMAP 3 year data; on scales of 4° the average temperature is lower, \(-73\mu K\). Using these two data points we derive an approximate relation between the temperature deviation and the corresponding size of the cold spot: \(\theta(\Delta T/T) \approx 4.5 \times 10^{-5}\), where \(\theta\) is the radius of the cold spot in degrees. We now perform an order of magnitude calculation to see if the late ISW can produce such a spot, assuming that the entire effect comes from the ISW.
The contribution of the late ISW along a given line of sight is given by \((\Delta T/T)_{ISW} = -2 \int \dot{\Phi} \, d\eta\), where the dot represents differentiation with respect to the conformal time \(\eta\), \(d\eta = dt/a(t)\), and \(a\) is the scale factor. The integrand will be non-zero only at late times \((z<1)\) when the cosmological constant becomes dynamically dominant.

We start with the Newtonian potential given by

\[ \Phi = GM/r \approx \frac{4\pi G}{3} r^2 \rho_b \delta. \]  

(4)

The proper size \(r\) and the background density \(\rho_b\) scale as \(a\) and \(a^{-3}\), respectively. The growth of the fractional density excess, \(\delta(a)\) in the linear regime is given by \(D(a) = \delta(a)/\delta(a_0)\), and \(D(a)\) is the linear growth factor. For redshifts below \(\sim 1\) in \(\Lambda\)CDM, this factor can be approximated as \(\delta(a) \approx a\delta(a_0)(3-a)/2\). Assuming that the region is spherical, its comoving radius is \(r_c = 0.5\Delta z(c/H)\), and \(\Delta z\) is the line of sight diameter of the region. The change in the potential over \(d\eta\) can be approximated by

\[ \Delta \Phi \sim \frac{4\pi G}{3} r_c^2 \rho_c \delta (\Delta z), \]  

(5)

where subscript \(c\) refers to the average comoving size of the void and the comoving background density. In \(\Lambda\)CDM the Hubble parameter is roughly given by \(H^2 = H_0^2(1 + 2z)\), for redshifts below \(\sim 1\). Incorporating these approximations we get the following relation between the size of the region, its redshift and the temperature deviation from the late ISW:

\[ \Delta \Phi \approx -\left( \frac{\Omega_m}{2} \right) \left( \frac{r_c}{c/H_0} \right)^3 (1 + 2z)^{1/2} (1 + z)^{-2} \delta \approx \frac{1}{2} \frac{\Delta T}{T}. \]  

(6)

We now ask under what conditions this expression is consistent with the observed relation between the size and temperature of the cold spot derived earlier, \(\theta(\Delta T/T) \approx 4.5 \times 10^{-5}\). For \(\Omega_m \sim 0.3\) and \(\delta = -1\) (i.e. a completely empty region) this leads to the simplified relation, \(\theta(1+z) \approx 6\), where \(\theta\) is in degrees, as before. Since the spot’s association with the NVSS places it at \(z \sim 0.5 - 1\), this leads to a self-consistent value of the radius of \(\sim 3 - 4^{\circ}\) for the observed spot. For \(c/H_0 = 4000\) Mpc, the comoving radius of the void region is 120-160 Mpc.

How likely is such a large underdense region in a concordance cosmology? Suppose there is only one such large underdense region in the whole volume up to \(z=1\). The corresponding void frequency is then the ratio of the comoving volume of the void to the comoving volume of the Universe to \(z=1\), which is roughly \(3 \times 10^{-5}\). Is this consistent with \(\Lambda\)CDM? Void statistics have been done for a number of optical galaxy surveys, as well as numerical structure formation simulations. Taking the most optimistic void statistics (filled dots in
Fig. 9 of Hoyle & Vogeley, 2004) which can be approximated by \( \log P = -(r/\text{Mpc})/15 \), a 140 Mpc void would occur with a probability of \( 5 \times 10^{-10} \), considerably more rare than our estimate for our Universe \( (3 \times 10^{-5}) \) based on the existence of the cold spot. One must keep in mind, however, that observational and numerical void probability studies are limited to \( r_c \sim 30 \) Mpc; it is not yet clear how these should be extrapolated to \( r_c > 100 \) Mpc.

We note that Inoue & Silk (2006a,b) had already suggested that anomalous temperature anisotropies in the CMB, such as the cold spot, may be explained by the ISW effect. In contrast to our calculation described above, their analysis considers the linear ISW plus the second order effects due to an expanding compensated void, partially filled with pressureless dust, embedded in a standard CDM (Inoue and Silk 2006a) or ΛCDM (Inoue and Silk 2006b) background. It is reassuring that the size of the void indicated by their analysis—about 200 Mpc if located at \( z \sim 1 \)—is roughly the same as what we get here using linear ISW.

The need for an extraordinarily large void to explain the cold spot would add to the list of anomalies associated with the CMB. (See Holdman, Mersini-Houghton & Takahashi (2006a,b) for a theory that predicts such large voids based on a particular landscape model.) These include the systematically higher strength of the late ISW correlation measured for a variety of mass tracers, compared to the WMAP predictions (see Fig. 11 of Giannantonio et al. 2006), and the alignment and planarity of the quadrupole and the octopole (de Oliveira-Costa et al. 2004; Land & Magueijo 2005). We can, however, conclude that models linking the cold spot with the larger scale anomalies, such as the anisotropic Bianchi Type VII\(_h\) model of Jaffe et al. (2005), are no longer necessary. While we suggest that the cold spot is a local effect, low order global anisotropic models (e.g., Gumrukcuoglu, Contaldi & Peloso 2006) may still be needed for the low—\( \ell \) anomalies.

5. Concluding Remarks

We have detected a significant dip in the average surface brightness and number counts of radio sources from the NVSS survey at 1.4 GHz in the direction of the WMAP cold spot. The deficit of extragalactic sources is also seen in a single dish image at 408 MHz. Together with previous work, we rule out instrumental artifacts in WMAP due to foreground subtraction. A fuller examination of the statistical uncertainties associated with our combination of the McEwen et al. (2007) wavelet results and our own a posteriori analysis should be performed. With this caveat, we conclude that the cold spot arises from effects along the line of sight, and not at the last scattering surface itself. Any non-gaussianity of the WMAP cold spot therefore would then have a local origin.
A 140 Mpc radius, completely empty void at $z \leq 1$ is sufficient to create the magnitude and angular size of the cold spot through the late integrated Sachs-Wolfe effect. Voids this large currently seem improbable in the concordance cosmology, adding to the anomalies associated with the CMB.

We suggest that a closer investigation of all mass tracers would be useful to search for significant contributions from isolated regions. Also, if our interpretation of the cold spot is correct, it might be possible to detect it indirectly using Planck, through the lack of lensing-induced polarization $B$ modes (Zaldarriaga & Seljak 1997).

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Fig. 1.— 50° field from smoothed NVSS survey at 3.4° resolution, centered at $l_{II}, b_{II} = 209^\circ, -57^\circ$. Values range from black: 9.3 mJy/beam to white: 21.5 mJy/beam. A 10° diameter circle indicates the position and size of the WMAP cold spot.
Fig. 2.— Aitoff projection of NVSS survey, centered at $l_{II}, b_{II} = 180^\circ, 0^\circ$, showing the median brightness in sliding boxes of 3.4°. The WMAP cold spot is indicated by the black box. Closer to the plane, large dark patches arise from sidelobes around strong NVSS sources.

Fig. 3.— The cumulative distribution, normalized to 1000, of median brightness levels (mK) in 3.4° sliding boxes of the NVSS images in two strips above $|b_{II}| > 30^\circ$ (see text). The minimum brightness (which is from the cold spot region) is indicated by a vertical line.
Fig. 4.— 18° fields, with 1° resolution, centered at $l_{II}, b_{II} = 209^\circ, -57^\circ$. Left: 408 MHz (Haslam et al. 1981). Right: 1.4 GHz (Condon et al. 1998). A 10° diameter circle indicates the position and size of the WMAP cold spot.
Fig. 5.— Number of NVSS sources in 3.14 square degree annuli as a function of distance from the cold spot. The counts axis refers to the results for counts of sources with $S>5\text{mJy}$; the grey line refers to counts for $S>2.5\text{mJy}$ with those counts multiplied by 0.56. Each bin is independent.